

Collapse and final explosions

Stars with initial mass of **less** then $\sim 8M_{\odot}$ (this limit depends strongly on mass loss) develop **degenerate cores** and if shell sources cannot increase M_c to M_{ch} the star becomes a WD. Other stars undergo core collapse (such as those with neutron stars as remnants) or explosions, thereby ejecting a large part of their mass (supernova).

Evolution of the C-O core

- Further evolution details depend on whether C-O core becomes degenerate or not in the ensuing contraction phase.
- Estimating critical core mass M_{crit} , which determines whether contraction will increase T_c , or if the core becomes degenerate:

consider (approximate) EOS interpolating between both (non-deg. – degen.) regimes:

P dominated by non-deg., e⁻ rel. ($\mu_e \approx z$, $\lambda \approx 12$)

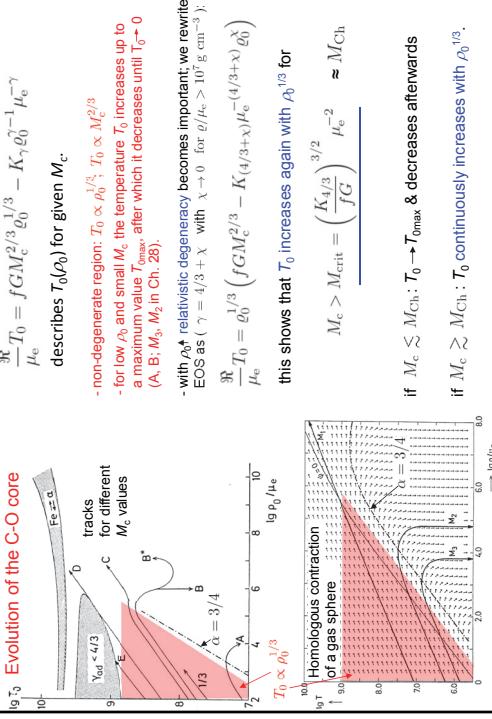
$$P \approx P_e = \frac{\mathfrak{R}}{\mu_e} \vartheta T + K_{\gamma} \left(\frac{\varrho}{\mu_e} \right)^{\gamma}$$

use EOS for P_e

$$\frac{\mathfrak{R}}{\mu_e} T_0 = f G M_c^{2/3} \varrho_0^{1/3} - K_{\gamma} \varrho_0^{\gamma-1} \mu_e^{-\gamma}$$

both terms are about equal for high-degeneracy

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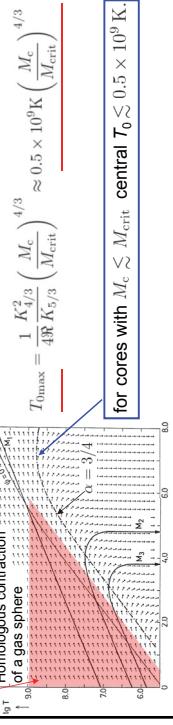
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estimate T_{max} for $M_c < M_{\text{crit}}$ in non-relativistic regime:

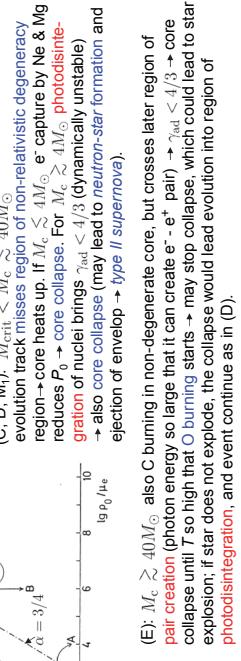
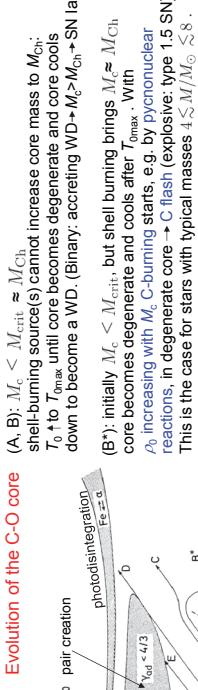
$$\frac{\mathfrak{R}}{\mu_e} T_0 = f G M_c^{2/3} \varrho_0^{1/3} - K_{\gamma} \varrho_0^{\gamma-1} \mu_e^{-\gamma}$$

$$M_{\text{crit}} = \left(\frac{K_{4/3}}{f G} \right)^{3/2} \mu_e^{-2}$$

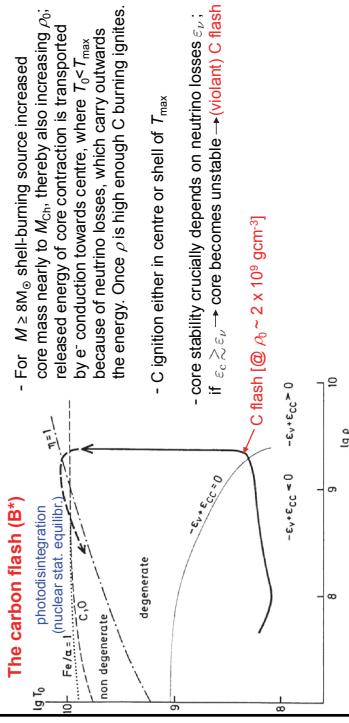
$$\gamma = 5/3$$



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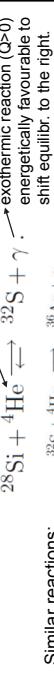
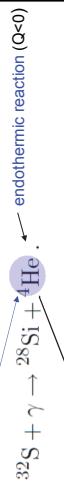
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Photodisintegration and nuclear statistical equilibrium

@ T about 10^9 - 10^{10} K photons γ so energetic (MeV) as to cause photodisintegration (photodissociation) in the nuclei in the gas (α decay), such as, for example,



Similar reactions:



Processes occur essentially in equilibrium (EQ) with similar numbers of nuclei being dissociated and created; EQ is eventually shifted to heavier nuclei ($> E_b$):

quasi-equilibrium processes (misleadingly called **silicon burning**).

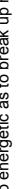
Similar reaction(s):
(neon burning)



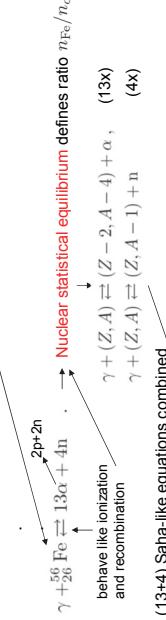
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Nuclear statistical equilibrium (in a plasma of photodisintegration)

@ T about 10^{10} K photons γ so energetic as to break up nuclei by α decay, e.g.:



^{56}Fe plays important role, because it is the nucleus with highest binding energy.



$$(1) \frac{n_\alpha n_u}{n_{\text{Fe}}} = \frac{C_\alpha^4 G_u^4}{G_{\text{Fe}}} \left(\frac{2\pi kT}{h^2} \right)^{24} \left(\frac{m_\alpha m_u}{m_{\text{Fe}}} \right)^{3/2} e^{-Q/kT} \quad \text{with } Q = (13m_\alpha + 4m_n - m_{\text{Fe}})c^2$$

where G_α , G_u and G_{Fe} are the statistical weights, while Q is the difference of binding energies

$$Q = (m_\alpha + m_u - m_{\text{Fe}})c^2 .$$

$$\text{also } (2) \rho = m_u \sum_i A_i n_i = (56n_{\text{Fe}} + 4n_\alpha + n_n)m_u$$

Note: for ^{56}Fe : $n_p/n_u = 13/15$

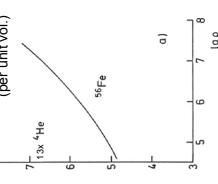
$$n_n/n_\alpha = 4/13$$

for given ratio, e.g. $n_n/n_\alpha = 4/13$ (^{56}Fe), 2 equ. (1)+(2) for 2 unknowns n_{Fe} and n_α .

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Nuclear statistical equilibrium (in a plasma of photodisintegration)

- ② T about 10^{10} K photons γ so energetic as to create $e^- - e^+$ pairs = photodisintegration, e.g. for given ratio, e.g. $n_n/n_\alpha = 4/13$ (^{56}Fe), and given ρ & T , nuclear equilibrium demands:

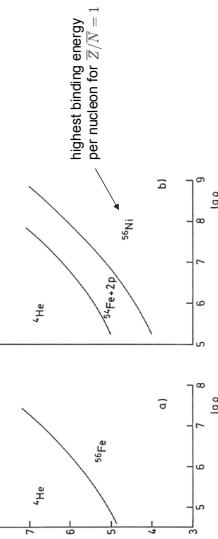
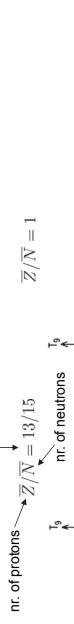


In nuclear statistical equilibrium at moderate T one expects nuclei of the iron group, which with increasing T disintegrate into α particles, protons and neutrons.

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Hydrostatic and convective adjustment during C flash

- during He flash star stays very close in hydrostatic equilibrium: convection removes energy.
- for **C flash** the situation is very different:
in a single thermal run away, after the C flash (ε_{CC}), T^* so fast that additional reactions (O burning) take place, core regions is then so hot that statistical equilibrium between Fe & He is reached \rightarrow degeneracy is removed, pressure increases \rightarrow central regions expand.
- **time scale** τ_ε determined by change of T & internal energy ($\dot{T}/T \simeq \varepsilon_{CC}/u$): $\tau_\varepsilon \simeq \frac{c_p T}{\varepsilon_{CC}} \simeq \frac{(G\rho)^{-1/2}}{\varepsilon_{CC}}$

other (outer) core regions react on the hydrostatic time scale :

- if $\zeta := \tau_\varepsilon/\tau_{hyd} >> 1 \rightarrow$ core follows expansion quasi-hydrostatically
 $\zeta << 1 \rightarrow$ outer layers can not expand rapidly enough,
compression wave will move outwards with c_s (outwards travelling shock wave)

convection in core will (a) transport part of surplus energy to outer layers,
(b) bring new fuel into burning layers.

- if $\zeta := \tau_\varepsilon/\tau_{conv} >> 1 \rightarrow$ convection carries all energy away from core
 $\tau_{conv} \simeq \ell_m/v_c$

in core $\rho > 10^8 \text{ g cm}^{-3}$, $T \simeq 3 \times 10^9 \text{ K}$ one typically finds $\tau_\varepsilon \simeq 10^{-6} \text{ s}$, $\tau_{hyd} \simeq 0.1 \text{ s}$ & $\tau_{conv} \simeq 0.1 \text{ s}$.
 $\rightarrow \zeta << 1$, & $\zeta << 1$ compression wave will start outwards and 'convective blocking' (strong damping if motion is $v_c \simeq c_s$) limits spread of energy released in the core.

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Combustion fronts (during C flash)

- $\tau_\varepsilon \simeq 10^{-6} \text{ s}$ at the onset is rather short \rightarrow burning proceeds at such high rates that fuel in mass shells consumed essentially instantly & layer above has not time to adjust.

layer ahead is heated to ignition either by compression or energy transport, and flash proceeds outwards (burning confined to very thin layer) \rightarrow outward moving combustion front.

- Two different types of combustion front:

- (a) matter in front enters discontinuity of compression wave (shock wave) with supersonic velocity and is compressed & heated; if matter is ignited combustion front coincides with shock front \rightarrow **detonation front**
- (b) if compression in shock wave does not ignite the fuel, then ignition temperature is reached due to energy transport (convection or conduction) \rightarrow slower subsonic motion of the burning front with a discontinuity in pressure and density drop (inwards) \rightarrow **deflagration front**

\rightarrow speed it controlled by energy transport (convection or conduction).

in both cases deviation from hydrostatic equilibrium mainly confined in thin shell of P, ρ discontinuity, and energy release.

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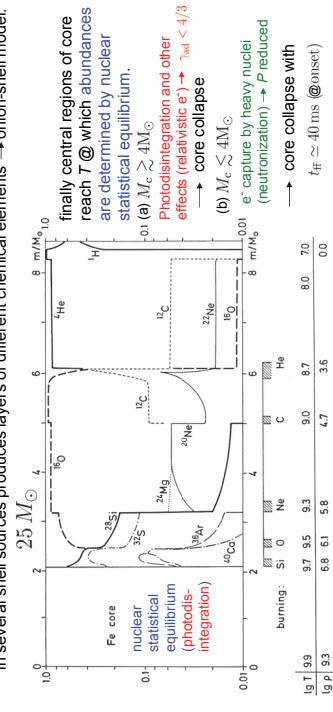
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Collapse and final explosions

Collapse of cores of massive stars (C,D): $M_{\text{Ch}} < M_c \lesssim 40M_\odot$

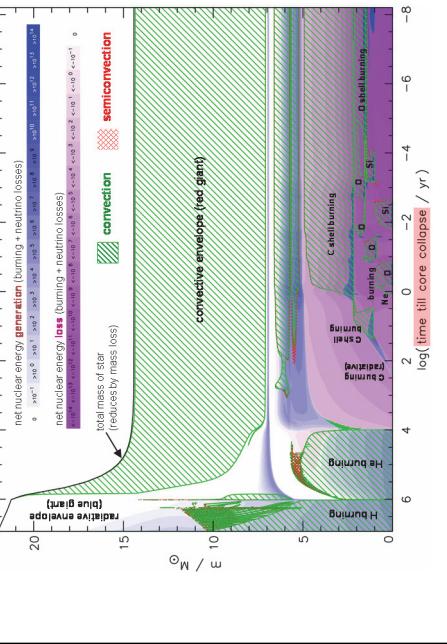
core 'misses' non-relativistic degeneracy and heats up during contraction until ignition of next heavier element. Core is then either non-degenerate (large M_c) or degenerate, but still in a region "above" $\alpha=4/3$, i.e. gravothermal heat capacity $C^* < 0 \rightarrow$ burning is stable!

after several cycles of nuclear burning and contraction, core will heat up to Si burning; burning in several shell sources produces layers of different chemical elements → onion-shell model.



Collapse and final explosions

Collapse of cores of massive stars (C,D): $M_{\text{Ch}} < M_c \lesssim 40M_\odot$



Collapse and final explosions

Reflection of infall (massive stars: C,D)

Because of infall ρ approaches that of neutron stars ($\rho \approx 10^{14} \text{ g cm}^{-3}$). Matter becomes incompressible (EOS is stiff).

Complete elastic reflection would bring whole collapse only to original state before the collapse; we need extra energy to expel the envelope.

Remnant (neutron star) is somewhat compressed by inertia beyond equilibrium state and afterwards, acting like a 'spring', it expands and pushes back the infalling matter.

This creates a pressure wave, steepening if it enters regions of lower density.

However, a substantial fraction of the energy in this **rebounded pressure wave** will be used up to disintegrate remaining Fe (in envelope) into free nucleons, i.e. only a small fraction of the (rebounced) kinetic energy remains in the shock wave for lifting the envelope (also major energy loss due to **neutrinos** → only 1% of initial kinetic energy available for lifting envelope).

During (core) collapse, neutrino production by **neutronization** becomes dominant. Because of large density, matter becomes opaque to neutrinos, i.e. free-mean path is reduced and so the neutrino velocity [for $\rho > 3 \times 10^{11} \text{ g cm}^{-3}$] neutrinos are trapped, because their velocities are smaller than the infall velocity (free-fall)] → influence further **neutronization**, i.e. **neutronization stops @ $\rho \sim 3 \times 10^{12} \text{ g cm}^{-3}$ (β equilibrium). Collapse stops @ $\rho > 10^{14} \text{ g cm}^{-3}$.**

In summary:
the pressure and energy loss due to electron capture accelerates the contraction (collapse).

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Neutrinos in MeV range have mean free path ($\mu=1$)

$$\ell_\nu = \frac{1}{n\sigma_\nu} = \frac{\mu m_u}{\varrho \sigma_\nu} \approx \frac{2 \times 10^{20} \text{ cm}}{\varrho}$$

Shock is formed at sphere labelled "Core shock", within which matter is almost at rest, after sudden stop of core collapse, once density has reached nuclear matter density ($\varrho \sim 10^10 \text{ g cm}^{-3}$). Neutrinos interact with electrons (inelastic scattering) and neutrinos are thermalized, which brings also the weak interaction into equilibrium (already at $\varrho \sim 10^{12} \text{ g cm}^{-3}$) - homologous core. Sound speed in core is larger than initial velocity. Where both velocities are the same = core shock boundary of homologous core. Thus the **sudden stop of collapse causes shock wave at the surface of the homologous core with $R \sim 30 \text{ km}$.**

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Reflection of infall (massive stars: C,D) : Supernova explosion

Shock wave travels outwards through rest of collapsing iron core with energy of about 10^{52} erg . Matter through which shock travels will be dissociated.

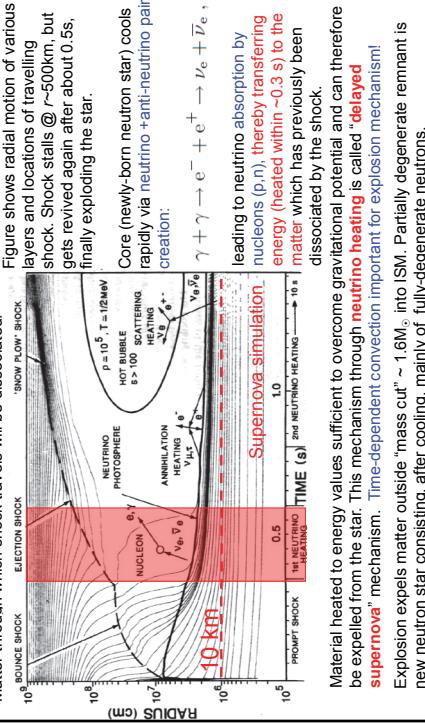


Figure shows radial motion of various layers and locations of travelling shock. Shock stalls @ $r \sim 500 \text{ km}$, but gets revived again after about 0.5s, finally exploding the star.

Core (newly-born neutron star) cools rapidly via neutrino + anti-neutrino pair creation:

$$\gamma + \gamma \rightarrow e^- + e^+ \rightarrow \nu_e + \bar{\nu}_e ,$$

leading to neutrino absorption by nucleons (p,n), thereby transferring energy (heated within $\sim 0.3 \text{ s}$) to the matter which has previously been dissociated by the shock.

Material heated to energy values sufficient to overcome gravitational potential and can therefore be expelled from the star. This mechanism through **neutrino heating** is called "**delayed supernova**" mechanism. Time-dependent convection important for explosion mechanism!

Explosion expels matter outside "mass cut" $\sim 1.6M_{\odot}$ into ISM. Partially degenerate remnant is new neutron star consisting, after cooling, mainly of fully-degenerate neutrons.

Some properties of Supernovae (SN)

SN are amongst the brightest objects in the universe and can be brighter than a whole galaxy for weeks.

Energy of visible explosion: $\sim 10^{51} \text{ erg}$ (= 1 foe [10^{50} erg])

Total energy : $\sim 10^{53} \text{ erg}$ (most in neutrinos)

Luminosity : $\sim 10^{9-10} L_{\odot}$

SN events are rather rare: some 1 – 10 per century and galaxy.
(In our Galaxy only a few have been recorded, the last one in the 17th century: Kepler's SN, type Ia).

Classifications of Supernovae (SN)

Observational:

- Type I : no H lines (depending on other spectral features: Ia, Ib, Ic,...)
- Type II : hydrogen lines

SN progenitor

- Type I : 2 possibilities
 - Ia : white dwarf accreting matter from (massive) companion in binary system
 - Ib,c: collapse of Fe core in star that blew its H (or He) envelope into space before the explosion
- Type II : collapse of Fe core in normal massive stars (8 – 30 M_{\odot})
- electron-capture SN (Crab nebula?)

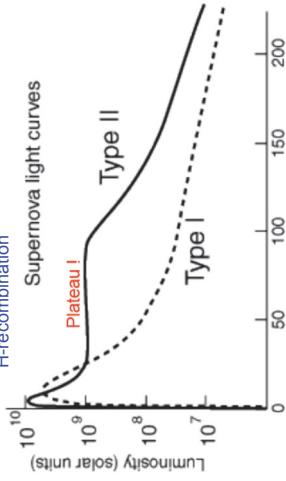
Classifications of Supernovae (SN)

Observational:

Type I		Type II		Type Ib/c		Type Ia	
Type I	No hydrogen	Type II-P/L	Type II-L	Type Ib	Type Ic	Type Ia	Type Ia
		Spectrum throughout	Shows hydrogen	Shows a nonionized helium (He^+) line at 587.6 nm	Weak or no silicon absorption feature	Presents a singly ionized silicon (Si^{+}) line at 615.0 nm (nanometers), near peak light	Shows a nonionized helium (He^+) line at 615.0 nm (nanometers), near peak light
						Core collapse	Thermal runaway
						Type I-P	Type Ia
						Reaches a "plateau" in its light curve	H-recombination
						No narrow lines	radiative decay: $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{56}\text{Fe}$
						Type I-L	
						Displays a "linear" decrease in its light curve (linear in magnitude versus time) [1]	
						Type IIn	
						Some narrow lines	

Classifications of Supernovae (SN)

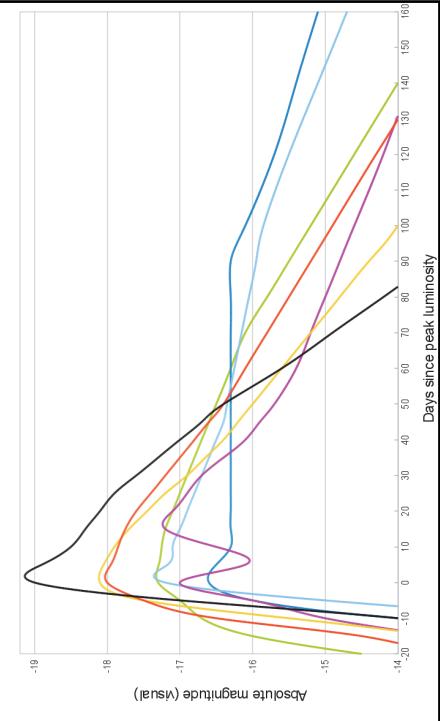
Energy sources: explosion
H-recombination
radiative decay: $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{56}\text{Fe}$



Adapted from Challisson & McMillan

Classifications of Supernovae (SN)

— Type Ia — Type Ib — Type Ic — Type IIb — Type II-L — Type I-P — Type IIn



Supernova explosion

