

Evolution on the asymptotic giant branch (AGB)

Evolution towards AGB

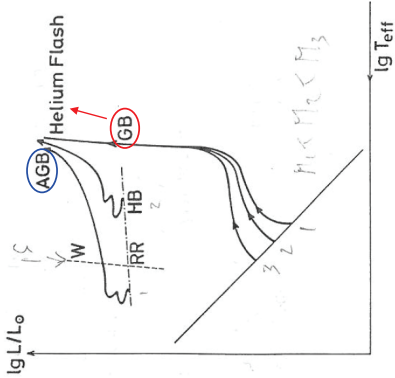
HB crosses IS → RR Lyrae variables (HB-pulsating stars), post-HB evolution also crosses IS → type II Cepheids (BL Herculis, previously called pulsating W Virginis stars).

After core-He-burning has ended the H-shell continues burning **outwards** until T_1 → **stops burning** → **E-AGB** (early AGB). For $M > 4M_\odot$ surface convection zone (envelope expansion) reaches layers of extinguished H-burning shell, thereby bringing H-burning ashes to surface → **2nd dredge up**.

He-shell burning layer still grows in mass approaching H-rich envelope → H-burning re-ignited → **again two shell source**, but **shell burning becomes secularly unstable** → **thermal runaway**.

(geometrical effect)

cyclic phenomenon – **thermal pulses** ($\Pi \sim 10^5$ y)



Evolution on the asymptotic giant branch (AGB)

(low-mass stars: $M < 2.3 M_\odot$)

Iben (1985; QJ. J. R. astr. Soc. 26, 1) evolution of a $2M_\odot$ star, losing $\sim 1.2M_\odot$ after AGB phase via ordinary wind & PN (thermal) pulses (**T-AGB**) are more or less an envelope phenomenon with **no influence on core**.

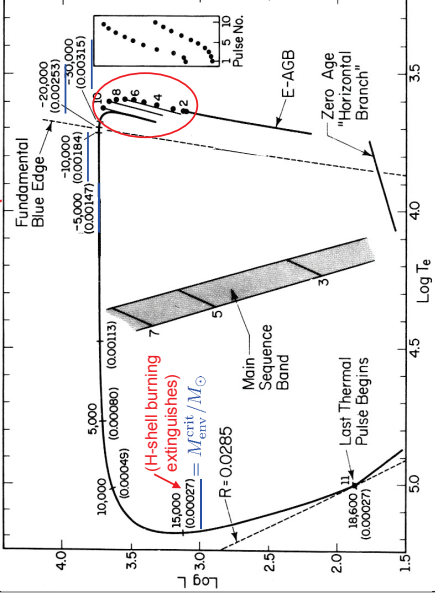
inner part of C-O core resembles more and more a **white dwarf**.

H-rich envelope, small in M but thick in R , gives appearance of a red giant.

However, during **thermal pulses** envelope **loses mass** from surface, which is ejected into space; additional **mass loss** due to H-burning @ bottom.

Envelope shrinks and within $\sim 10^4$ y star moves to the left (**post-AGB**).

H-shell burning extinguishes (M_{env} drops below $0.00027M_\odot$) and the star becomes a white dwarfs (WD).



An originally $2M_\odot$ star develops a C-O core of $\sim 0.6M_\odot$; Planetary Nebula (PN) ejection (superwind) occurs at \sim the 10th pulse. When T_{surf} of star reaches $\sim 30,000\text{K}$ ($\alpha \neq 0$), photons emitted from surface are 'hard' enough to ionize surrounding nebular shell. The star is then called a Planetary Nebular Nucleus (PNN).

Evolution on the asymptotic giant branch (AGB)

Shell sources and their stability

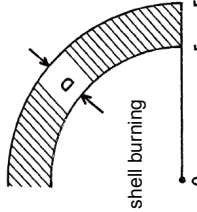
Evolved stars can have several shell sources (H, He, ...), which burn farther out, towards the surface, with time. While burning outwards, the shell sources have the tendency to concentrate the reactions over steadily decreasing mass ranges. The thickness D of the shell source starts playing a role in both computational issues (time step) and (shell source) stability. Procedure for stability consideration is similar to central nuclear burning but with 2 differences:

(a) the geometry (thickness D) and (b) the density reaction $d\rho/\rho$ to an expansion $dr/r > 0$.

$$r = r_0 + D \quad m \sim \rho r_0^2 D \quad ; \quad D/r_0 \ll 1$$

burning region expands with roughly $r_0 = \text{constant}$: $dr = dD$

$$\frac{d\rho}{\rho} = -\frac{dD}{D} = -\frac{r dr}{D r}$$



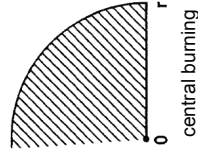
assume mass outside $r_0 + D$ expands homogeneously ($\dot{r}/r = \text{const.}$):

$$c^* \frac{dT}{dt} = d\varepsilon; \quad c^* = c_P \left(1 - \nabla_{\text{ad}} \frac{4\delta}{4\alpha - r/D} \right)$$

if $c^* > 0$ shell source unstable, because any $\varepsilon > 0$ leads to an increase of T and further increased burning.

expansion $dr/r > 0$ requires density change of

$$m \propto \rho r^3 \rightarrow \frac{d\rho}{\rho} = -\frac{3dr}{r} \quad ; \quad dm = 0$$



Evolution on the asymptotic giant branch (AGB)

Shell sources and their stability

if $c^* > 0$ shell source unstable, because any $\varepsilon > 0$ leads to an increase of T and further increased burning.

$$c^* \frac{dT}{dt} = d\varepsilon; \quad c^* = c_P \left(1 - \nabla_{\text{ad}} \frac{4\delta}{4\alpha - r/D} \right)$$

We recover flash instability for strong degeneracy, i.e. with $\delta \rightarrow 0$, $c^* > 0$.

New instability even for an ideal monoatomic gas with $\alpha=1$, $\delta=1$, $\nabla_{\text{ad}} = 2/5$, which depends only on thickness D :

if $D/r < 1/4 \rightarrow c^* > 0 \rightarrow$ shell source is secularly unstable

→ pulse instability

because of $D/r < 1$ any substantial increase $dD/D > 0$ results in a relative density decrease $d\rho/\rho < 0$ of same absolute value, but only a very small relative increase dr/r , i.e. layers above are scarcely lifted, so that their weight remains about constant, i.e. $dP/P \approx 0$.

$$\frac{dP}{P} = -4 \frac{dr}{r} = -4 \frac{D}{r} \frac{d\rho}{\rho} \approx 0 \rightarrow \frac{d\rho}{\rho} = -\delta \frac{dT}{T} \rightarrow \rho \propto \frac{1}{T}$$

expansion $d\rho/\rho < 0$ leads to increase of T ($dT/T > 0$) → pulse instability

$\alpha = 0, \delta = 1, \rightarrow c^* > 0 \rightarrow$ pulse instability

Evolution on the asymptotic giant branch (AGB)

Thermal pulses of a shell source [occur in stars (models) with one or more shell sources.]

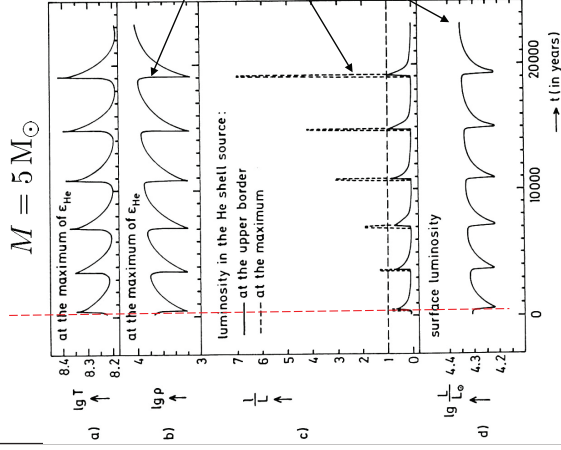
For $5M_{\odot}$ instability occurs in He shell source after it has reached $m/M \approx 0.1597$. It then contributes little to surface L , which is almost completely supported by near-by H-shell source @ $m/M \approx 0.1603$.

Instability results in thermal runaway: shell source reacts to surplus energy with $T \uparrow$, which enhances nuclear energy release even further. T increase connected with expansion $d\rho/\rho < 0$.

Note: in a flash $\rho = \text{const.}$, because of degeneracy! because $\epsilon_{\text{He}} \sim T^{19} \rightarrow l$ increases (up to several l) with most of energy used to expand outer layers ($T \uparrow$ in H shell $\rightarrow L_{\text{H}} \uparrow$).

thermal runaway accelerates more until reaching a sharp peak within a few years \rightarrow He-shell source is now widely expanded ($D/r > 1/4$) and therefore no longer unstable.

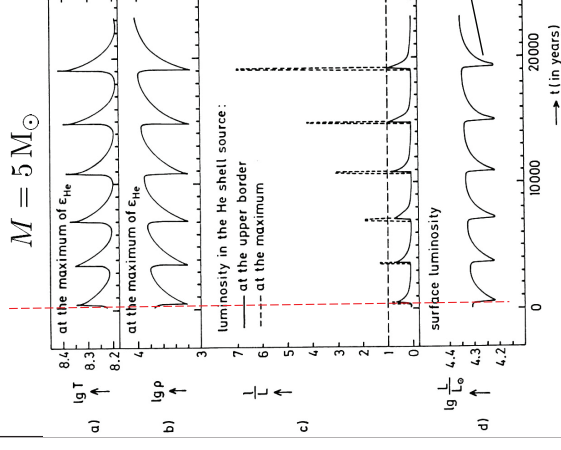
whole region starts to contract again, heating H-shell source & after few 10^3 y the He-shell source becomes unstable again \rightarrow next pulse, etc.



Surface luminosity L drops in each pulse by about $\Delta \lg L \approx 0.1 \dots 0.2$. Visible surface changes more pronounced if shell source is located close to surface.

Evolution on the asymptotic giant branch (AGB)

Thermal pulses of a shell source [occur in stars (models) with one or more shell sources.]



Period between consecutive pulses $\sim 3200 \dots 4300$ y.

Evolution on the asymptotic giant branch (AGB)

Iben (1985; QJ. J. R. astr. Soc. 26, 1) evolution of a $2M_{\odot}$ star, losing $\sim 1.2M_{\odot}$ after AGB phase via ordinary wind & PN

(thermal) pulses are more or less an envelope phenomenon with no influence on core.

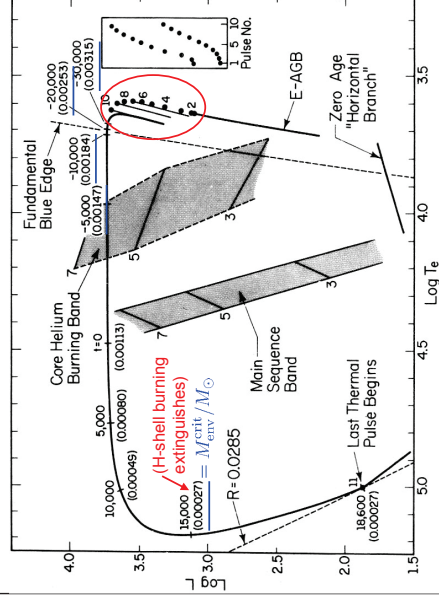
inner part of C-O core resembles more and more a white dwarf.

H-rich envelope, small in M but thick in R , gives appearance of a red giant.

however, during thermal pulses envelope loses mass from surface, which is ejected into space; additional mass loss due to H-burning @ bottom.

envelope shrinks and within $\sim 10^4$ y star moves to the left (WD-track).

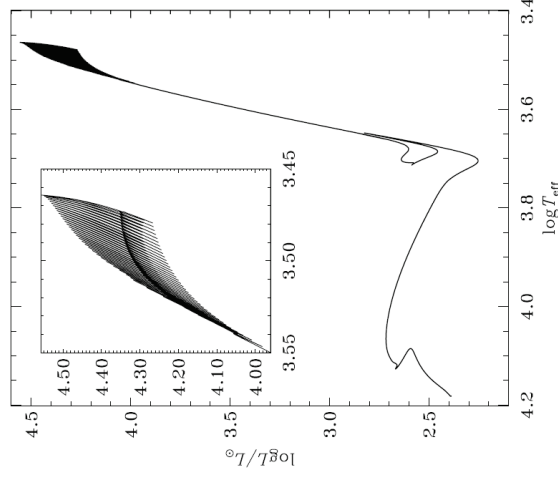
H-shell burning extinguishes (M_{env} drops below $0.00027M_{\odot}$) and the star becomes a white dwarfs (WD).



An originally $2M_{\odot}$ star develops a C-O core of $\sim 0.6M_{\odot}$; Planetary Nebula (PN) ejection (superwind) occurs at \sim the 10th pulse. When T_{surf} of star reaches $\sim 30,000\text{K}$ ($@t=0$), photons emitted from surface are 'hard' enough to ionize surrounding nebular shell. The star is then called a Planetary Nebular Nucleus (PNN).

Evolution on the asymptotic giant branch (AGB)

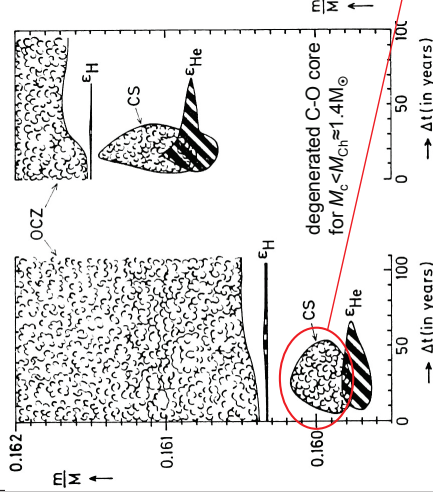
Thermal pulses also in more massive stars ($4M_{\odot}$)



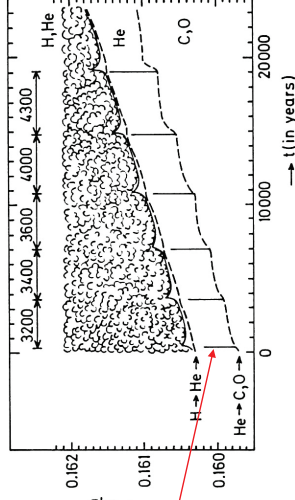
Evolution on the asymptotic giant branch (AGB)

Thermal pulses of a shell source: Nucleosynthesis on the AGB

high $\max(L)$ (peaks) create short-lived convective (inter-) shell (CS). Almost all matter between 2 shell sources (H, He) is mixed into He-burning shell (H down, C up).



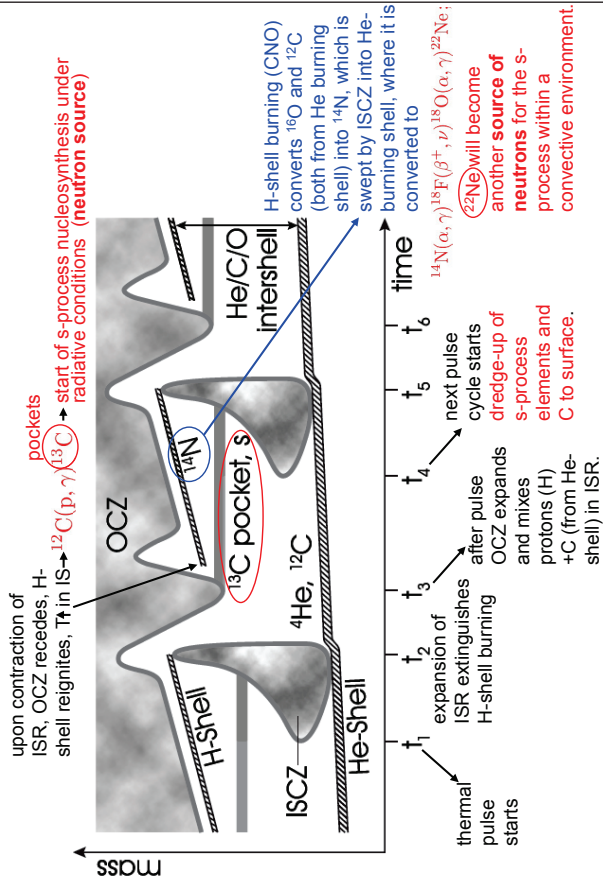
Outer convection zone (OCZ), can reach down to H-shell source and even beyond the H-He discontinuity into the inter-shell region → H-rich material is then transported downwards and inter-shell material to the surface → 3rd dredge up.



Evolution on the asymptotic giant branch (AGB)

Thermal pulses of a shell source: Nucleosynthesis on the AGB

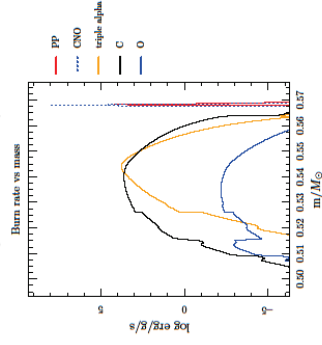
Sketch of additional mixing in inter-shell region (ISR) due to the inclusion of, e.g., OV, in order to produce observed surface abundance ratios of C/O > 1 (carbon stars), by "forcing" a 3rd dredge-up.



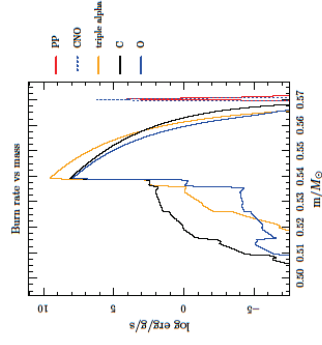
Evolution on the asymptotic giant branch (AGB)

MESA

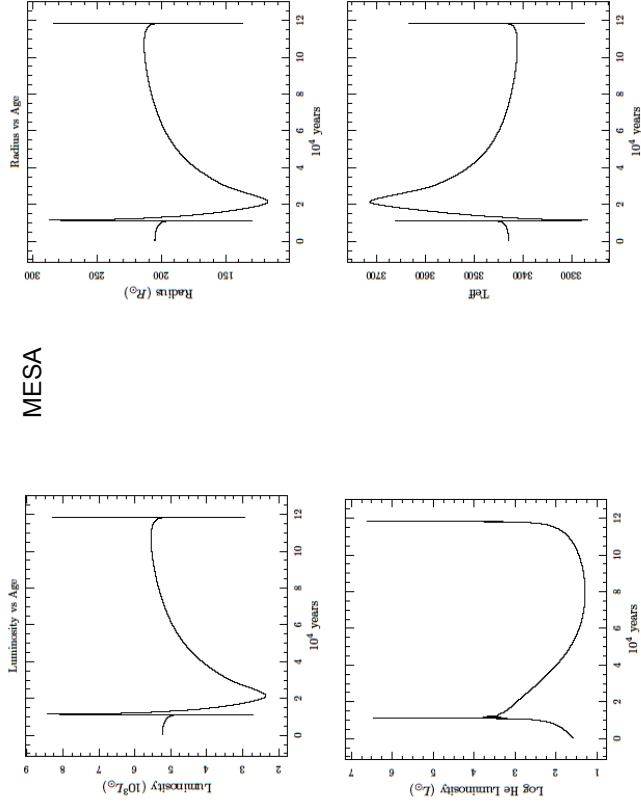
age = 92435 y



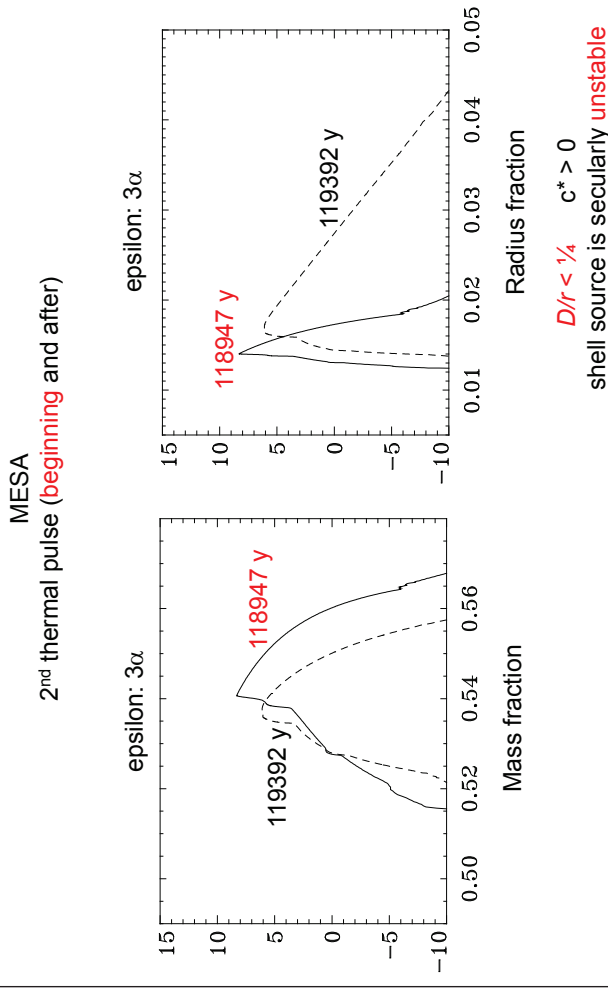
age = 118947 y



Evolution on the asymptotic giant branch (AGB)



Evolution on the asymptotic giant branch (AGB)



Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

Neutron sources for the s process

2 neutron-producing reactions available during He-shell burning:



- Requires the presence of both H and He in a He-burning region when normally there is no hydrogen
- Requires mixing of protons into He-burning region
- Occurs at $T \sim 100 \times 10^6 \text{ K}$, so in between thermal pulses, and under radiative conditions ($t \sim 10^4$ years)
- Dominant neutron source in low-mass AGB stars (1 to 3 M_{sun} stars)
- He-shell flashes imply many exposures to neutron source, produces heavy s-process elements $A > 80$

Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

Neutron sources for the s process

2 neutron-producing reactions available during He-shell burning:



- Plenty of ^{14}N left over from CNO cycling to produce the ^{22}Ne
- Occurs during thermal pulses when the temperature exceeds about $300 \times 10^6 \text{ K}$, under convective conditions
- These temperatures are not reached in the He-shells of low-mass AGB stars, except perhaps in the last few TP
- So only in:
 - a) the cores of massive stars ($M > 12 M_{\text{sun}}$)
 - b) massive AGB stars (~ 3 to $8 M_{\text{sun}}$) during He-shell flashes

Evolution on the asymptotic giant branch (AGB)
Nucleosynthesis on the AGB

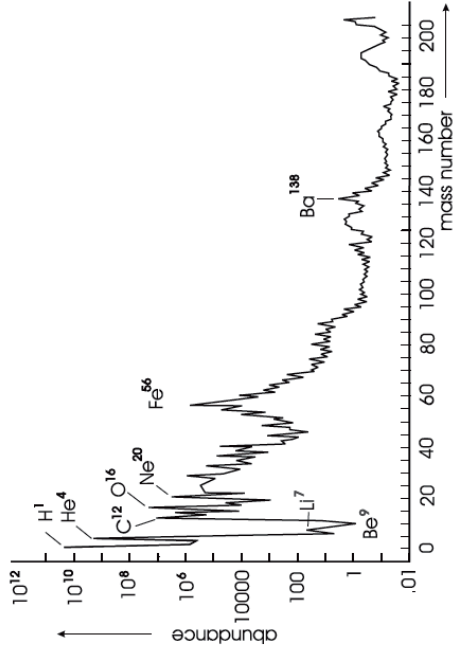


Fig. 18.9. The abundances (particle number fractions) of elements in the Sun, normalized to a value of 10^6 for ^{28}Si .

Evolution on the asymptotic giant branch (AGB)
Nucleosynthesis on the AGB

Neutron capture:



(followed by) β^- decay (if resulting nucleus is unstable);



β^- decay is a relatively slow process

or by another neutron capture leading to an even heavier isotope:

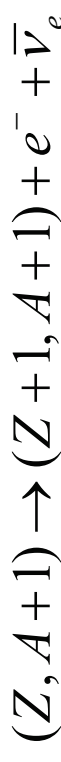


Evolution on the asymptotic giant branch (AGB)
Nucleosynthesis on the AGB

Neutron capture:



(followed by) β^- decay (if resulting nucleus is unstable):



or by another neutron capture leading to an even heavier isotope:



Evolution on the asymptotic giant branch (AGB)
Nucleosynthesis on the AGB

β^- decay

$p \leftrightarrow n$ conversion within a nucleus via weak interaction

Modes (for a proton/neutron in a nucleus):

β^+ decay	$p \rightarrow n + e^+ + \nu_e$	} Favourable for n-deficient nuclei (or p-rich)
electron capture	$e^- + p \rightarrow n + \nu_e$	
β^- decay	$n \rightarrow p + e^- + \bar{\nu}_e$	

Electron capture (or EC) of atomic electrons or, in astrophysics, of electrons in the surrounding plasma

Inverse β^- decay



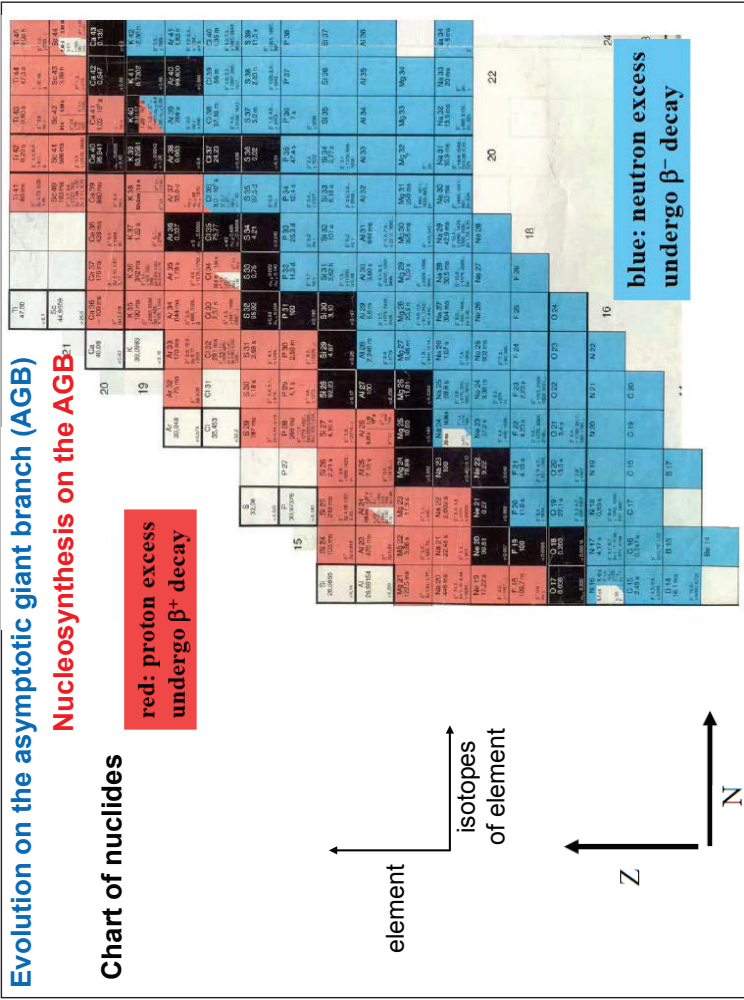
note: e^- capture is also sometimes referred to as inverse β^- decay.

Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

Typical β decay half-lives:

very near "stability": occasionally Mio's of years or longer
 more common within a few nuclei of stability: minutes - days
 most exotic nuclei that can be formed: ~ milliseconds

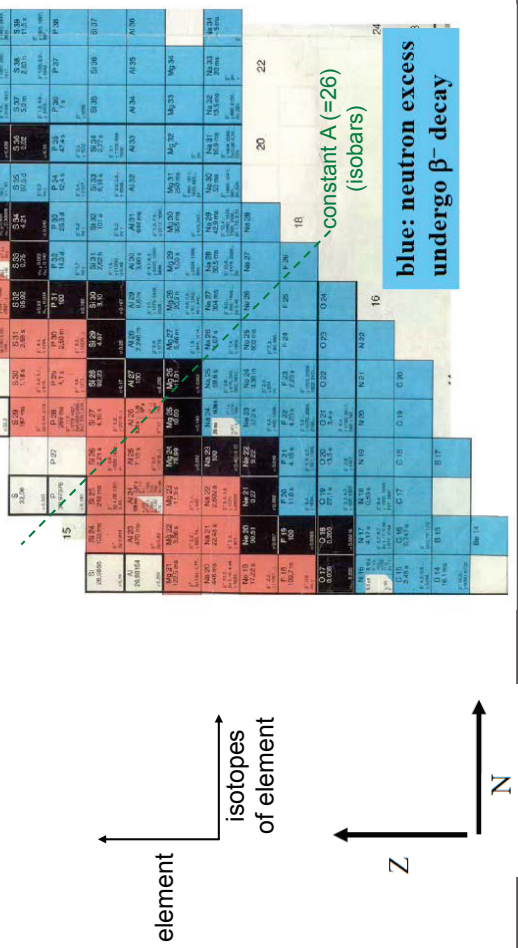


Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

Chart of nuclides

red: proton excess undergo β^+ decay

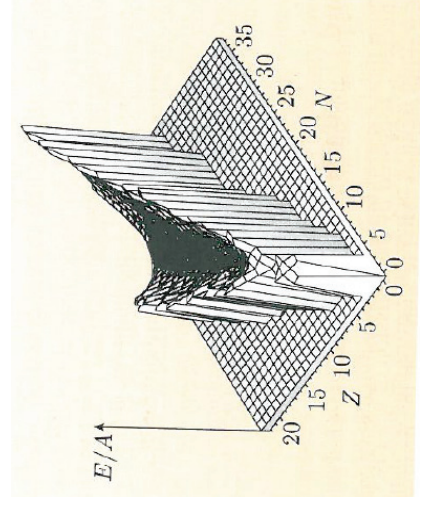


Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

The valley of stability

Binding energy per nucleon $f=E/A$



Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

2 types of neutron (n) capture:

(1) **s process** (for slow): where n capture is much slower (>1000 y) than β^- decay:



Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

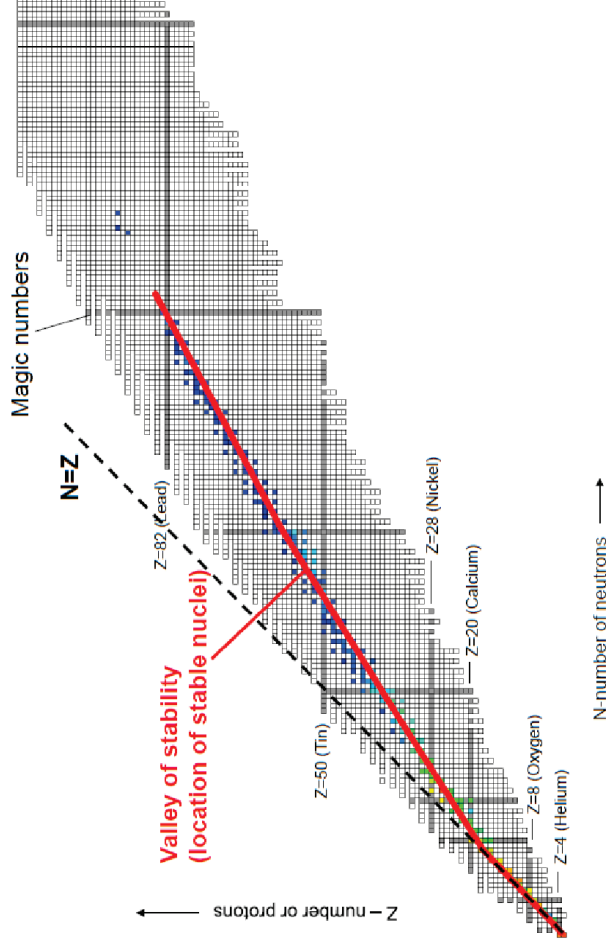
2 types of neutron (n) capture:

(2) **r process** (for rapid): where n capture is much faster (~1s) than β^- decay:



Evolution on the asymptotic giant branch (AGB)

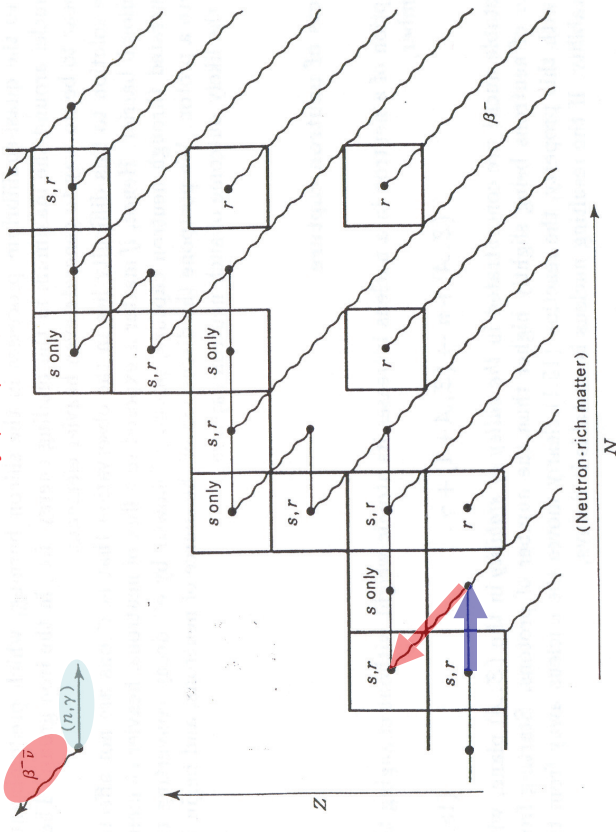
The valley of stability



Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

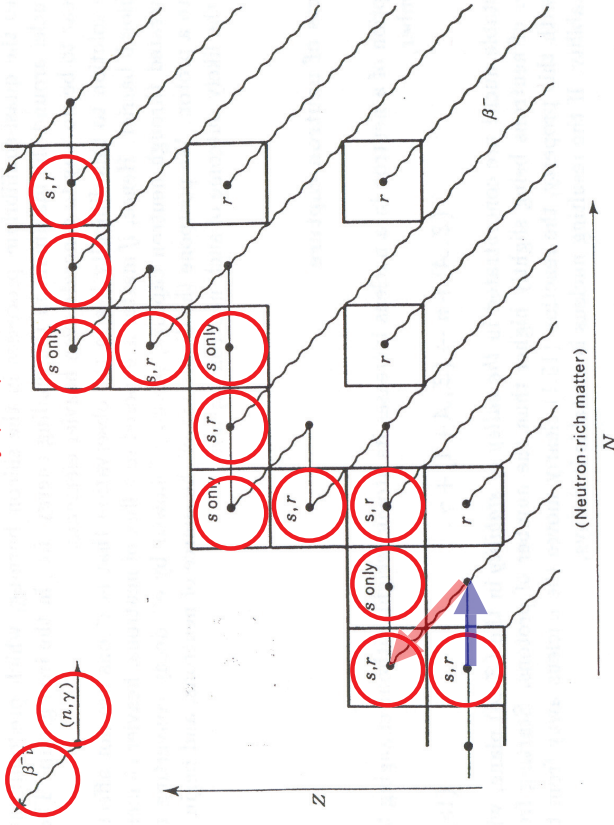
Low neutron density (flux): s process



Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

Low neutron density (flux): s process



Evolution on the asymptotic giant branch (AGB)

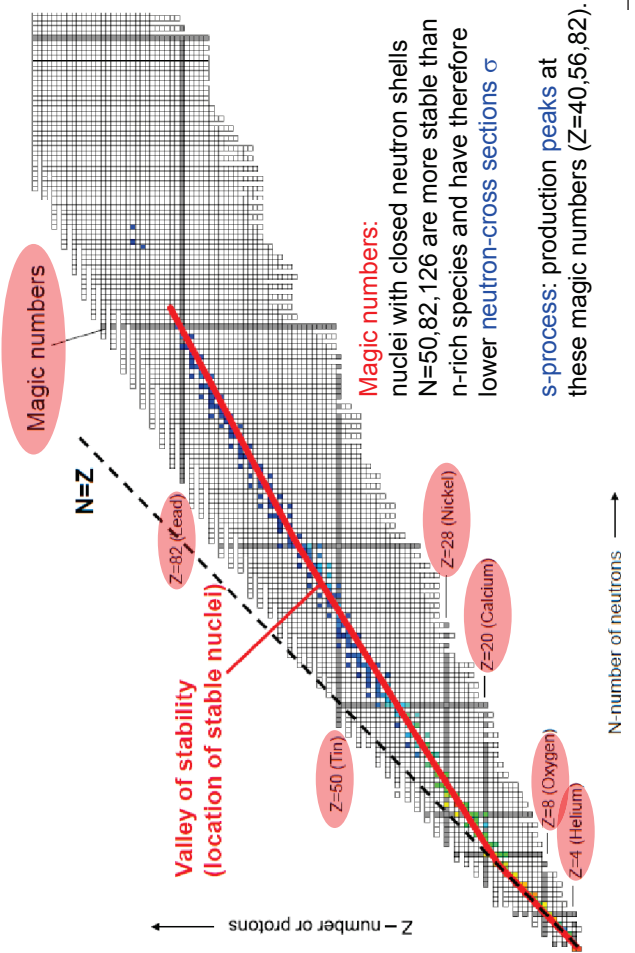
Nucleosynthesis on the AGB

Low neutron density (flux): s process

atomic number Z	neutron number N									
	44	46	48	50	52	54	56	58	60	62
88Sr	16.5 hrs	1.68 hrs	83.4 hrs	78.41 hrs	51.5 yrs	11.2% 17.2% 10 ⁸ yrs	17.4% 16.91 yrs	10.3 hrs	10.3 hrs	5.34 s
89Y	2.68 hrs	14.71 hrs	79.5 hrs	106.65 hrs	100% 64.10 days	58.51 hrs	18.7 hrs	10.3 hrs	5.34 s	1.5 s
90Zr	64.84 hrs	64.84 hrs	9.9% 7.0% 82.6% 10 ⁸ yrs	82.6% 10 ⁸ yrs	82.6% 10 ⁸ yrs	28.78 hrs	7.423 hrs	75.3 s	4.02 s	1.5 s
91Nb	14.5 hrs	1.9 hrs	83.4 hrs	78.41 hrs	51.5 yrs	11.2% 17.2% 10 ⁸ yrs	17.4% 16.91 yrs	10.3 hrs	10.3 hrs	5.34 s
92Mo	15.49 hrs	14.8% 10 ⁸ yrs	9.3% 15.8% 16.7% 9.6% 24.1% 10 ⁸ yrs	9.3% 15.8% 16.7% 9.6% 24.1% 10 ⁸ yrs	9.3% 15.8% 16.7% 9.6% 24.1% 10 ⁸ yrs	9.3% 15.8% 16.7% 9.6% 24.1% 10 ⁸ yrs	9.3% 15.8% 16.7% 9.6% 24.1% 10 ⁸ yrs	9.3% 15.8% 16.7% 9.6% 24.1% 10 ⁸ yrs	9.3% 15.8% 16.7% 9.6% 24.1% 10 ⁸ yrs	9.3% 15.8% 16.7% 9.6% 24.1% 10 ⁸ yrs

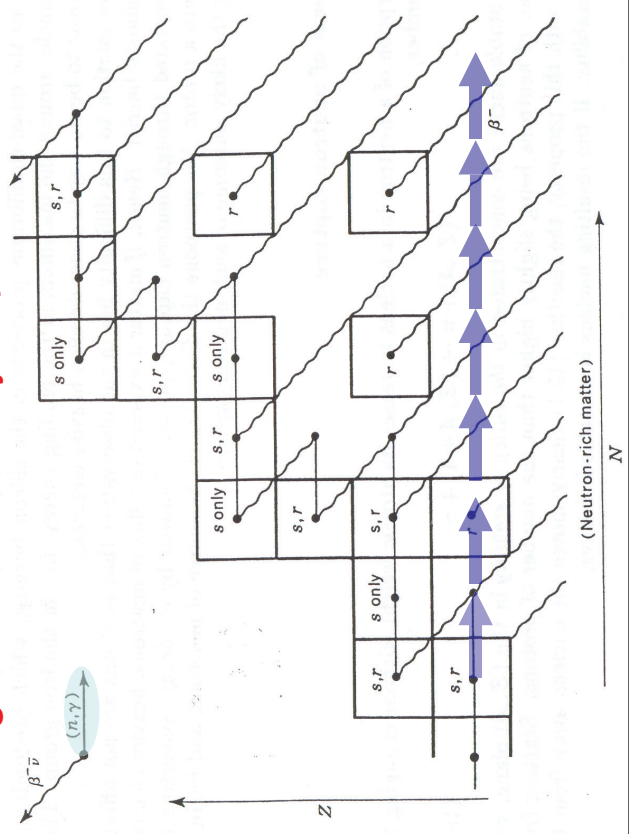
Evolution on the asymptotic giant branch (AGB)

The valley of stability



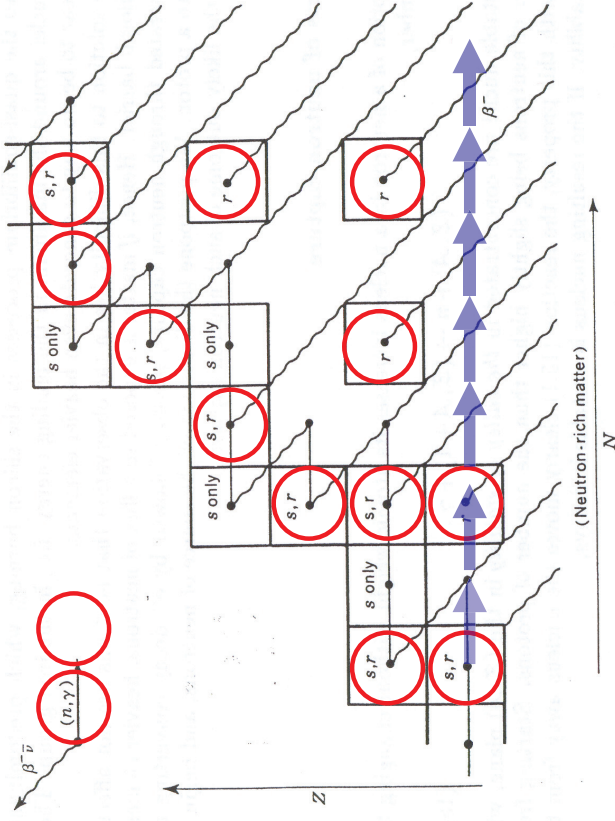
Nucleosynthesis

High neutron density: r process



Nucleosynthesis

High neutron density: r process

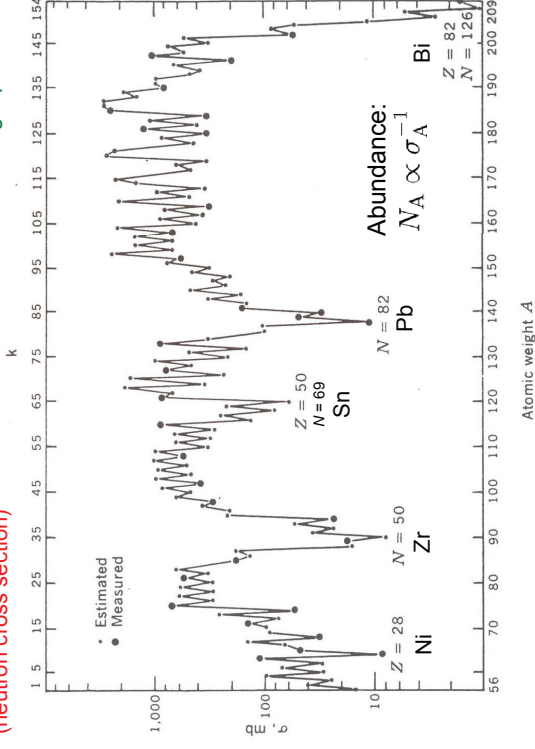


Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis

Approximate equilibrium between produced and destroyed isotopes:

rate of production of nucleus A from nucleus $A-1$ (neutron cross section) $\rightarrow \sigma_{A-1} N_{A-1} \simeq \sigma_A N_A$ \leftarrow rate of destruction of nucleus A
 \sim constant along s -path



Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

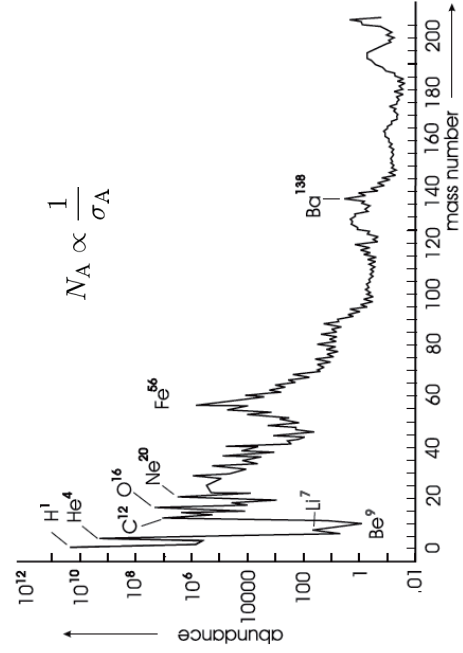


Fig. 18.9. The abundances (particle number fractions) of elements in the Sun, normalized to a value of 10^6 for ^{28}Si .

Evolution on the asymptotic giant branch (AGB)

Nucleosynthesis on the AGB

More accurate description shows that $\sigma_A N_A$ is a slowly varying function of A for nuclei created by the s process

